

1 Problem set 2: Hints & Tips

1.1 Formal solution of the radiative transfer equation

- re-use the class (or code) you wrote for the previous problem, in particular the tau grid and the infrastructure
- start by generating the points μ_j and weights w_j for the Gauss quadrature that replaces the J integration $J(\tau) = 1/2 \sum w_j I(\mu_j, \tau)$. There's a numpy method for this:
`self.mu, self.w = np.polynomial.legendre.leggauss(nmu)`
- You will need to write a routine that computes $I(j, i)$ for all μ_j and τ_i
- This is done by compute $I(j, :)$ for each j in succession by applying the scheme discussed in the lectures and the problem sheet.
- For this you need the coefficients $\alpha_i, \beta_i, \gamma_i$. The method `computeFScoeffs` in the template does that for you, you need to provide S_{i-1}, S_i, S_{i+1} in S_m, S_0, S_p and $\tau_{\text{prev} \rightarrow \text{curr}}$ and $\tau_{\text{curr} \rightarrow \text{next}}$ in $d\tau, d\tau_1$. Set `self.taulin=1e-2` and `self.use_Bezier = False`.
- It is easier to first (for a given direction μ_j) compute the $\alpha_i, \beta_i, \gamma_i$ for all i and store them in numpy arrays and then in a second step to compute the $I(j, i)$ for all i and given j .
- Keep in mind that the direction of solving changes depending on the sign of μ_j . For $\mu > 0$ you need to go from large τ towards zero, for $\mu < 0$ it is from zero to τ_{max} . Similar for γ . Remember that the solution follows the propagation of the photons. α always considers the previous point, that can be either $i-$ or $i+1$, depending on $\text{sign}(\mu_j)$.
- With the routine computing $I(i, j)$, the formal solution is now easy, just call it for the different j and compute $J(i) = \sum_j w_j I(j, i)$. Note: you do NOT need to store $I(j, i)$, just call your routine and the contributions for J on the fly. For this exercise it's easy to just store the full $I(j, i)$, but imagine you have millions of τ points (3D models!) and thousands of j ...
- In general, it is best to sketch the solution on a (big) sheet of paper. Think first, code later. In a variation of a quote from Stanislaw Lem: Think more, code less.